

SECTION-A

1. (A) $314\sqrt{2} \text{ cm}^2$

2. (C) 52.4 A

3. (A) 64

4. (C) 11.82 m^2

5. (D) $b^2 = a + 1$

6. (C) cosec A

7. (A) 2:5

8. (B) $10\sqrt{3} \text{ m}$

9. (C) 3.5 cm

10. (D) $\frac{AC}{BC} = \frac{PR}{QR}$

11. (C) 0.3

12. (D) $\frac{82}{80}$

13. (C) $\frac{10}{0.2}$

14. (B) $\frac{49}{12}$

15. (C) $a(x^2 + 5x - 24)$

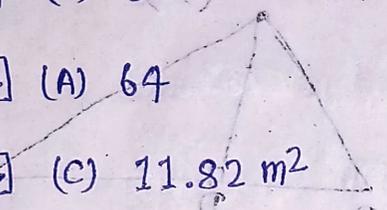
16. (B) -5

17. (C) 45°

18. (A) $\frac{5}{12}$

SECTION-B

10



(15) $8 \cdot (3.14) = 4$...

double ...
 divide ...
 $\left(\frac{10x+10}{1+x}\right) \cdot \left(\frac{10x+10}{1+x}\right) = 0$

$\left(\frac{10}{1} \pm 0\right) =$

length of AD = ...

$\frac{10x+10}{1+x}$

...

$\left(\frac{10}{1}\right) - \left(\frac{10}{1}\right) =$

$\left(\frac{10}{1}\right)$

$5 \times \left(\frac{1}{10} - \frac{10}{1}\right) =$

$\frac{10}{10} \times 5 = 5 \times \frac{10-10}{10} =$

19. (A)

20. (C)

SECTION-B

21.

In this ΔABC , $A=(1,5)$, $B=(-2,1)$ and $C=(4,2)$

D is a point of BC which divide in 1:2 ratio, then

$$D = \left(\frac{1(4) + 2(-2)}{1+2}, \frac{1(2) + 2(1)}{1+2} \right)$$

$$= \left(0, \frac{4}{3} \right)$$

Length of AD = $\sqrt{(1-0)^2 + (5-\frac{4}{3})^2}$

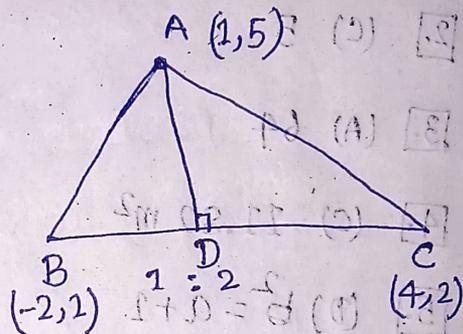
$$= \sqrt{1 + \frac{121}{9}} = \frac{\sqrt{130}}{3}$$

22. (a) $\frac{\sin^3 60^\circ - \tan 30^\circ}{\cos^2 45^\circ}$

$$= \frac{\left(\frac{\sqrt{3}}{2}\right)^3 - \left(\frac{1}{\sqrt{3}}\right)}{\left(\frac{1}{\sqrt{2}}\right)^2}$$

$$= \left(\frac{3\sqrt{3}}{8} - \frac{1}{3\sqrt{3}}\right) \times 2$$

$$= \frac{27-8}{24\sqrt{3}} \times 2 = \frac{19}{12\sqrt{3}}$$



(A) 1
 (B) 2
 (C) 3
 (D) 4
 (E) 5
 (F) 6
 (G) 7
 (H) 8
 (I) 9
 (J) 10
 (K) 11
 (L) 12
 (M) 13
 (N) 14
 (O) 15
 (P) 16
 (Q) 17
 (R) 18
 (S) 19
 (T) 20

22 (b) Given $\tan(A+2B) = \sqrt{3}$

$\Rightarrow A+2B = 60^\circ$ (i)

And $\sin(2A+B) = \frac{1}{\sqrt{2}}$

$\Rightarrow 2A+B = 45^\circ$ (ii)

Where $A, B, A+2B$ and $2A+B$ are acute angles.

Eqⁿ (i) $\times 2$: $A+2B = 60^\circ$

Eqⁿ (ii) $\times -1$: $-2A-2B = -90^\circ$

$3A = -30^\circ$

$\Rightarrow A = 30^\circ$

From (i) $A+2B = 60^\circ$

$\Rightarrow 2B = 60^\circ - 30^\circ$
 $= 30^\circ$

$\Rightarrow B = 15^\circ$

23.

A bag contains 25 balls.

Let no. of green balls = x .

one ball is drawn at random.

Given $P(\text{getting a green ball}) = \frac{3}{5}$

$\Rightarrow \frac{\text{no. of favourable events}}{\text{Total no. of outcomes}} = \frac{3}{5}$

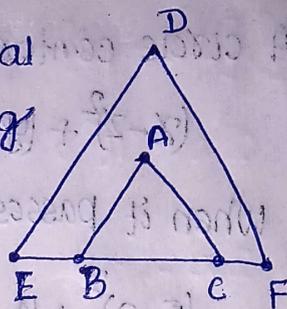
$\Rightarrow \frac{x}{25} = \frac{3}{5}$

$\Rightarrow x = 15$

Hence, number of green balls are 15.

24. Given $ED \parallel AB$ and EC is a transversal

then $\angle DEB = \angle ABC$ (corresponding angle)



Again $DF \parallel AC$ and BF is a transversal

then $\angle ACB = \angle DFC$ (corresponding angle)

In $\triangle ABC$ and $\triangle DEF$

$$\angle B = \angle E$$

$$\text{and } \angle C = \angle F$$

Hence by AA similarity criterion

$$\triangle ABC \sim \triangle DEF$$

$$\text{Again } \frac{BC}{EF} = \frac{AB}{DE} \Rightarrow DE = \frac{AB \times EF}{BC} = \frac{7 \times 20}{10} = 14 \text{ cm.}$$

25. Given $\sqrt{3}$ is irrational.

Suppose that $14 - 2\sqrt{3}$ is rational

$$\text{then } 14 - 2\sqrt{3} = \frac{p}{q}; \text{ where HCF}(p, q) = 1$$

$$\Rightarrow 2\sqrt{3} = 14 - \frac{p}{q}$$

$$\Rightarrow \sqrt{3} = 7 - \frac{p}{2q}$$

but $\sqrt{3}$ is irrational and $7 - \frac{p}{2q}$ is rational

which is a contradiction.

Hence $14 - 2\sqrt{3}$ is irrational.

26. (a) A circle centered at $(2, 1)$ is

$$(x-2)^2 + (y-1)^2 = r^2 \quad \text{--- (i)}$$

When it passes through $A(5, 6)$

$$(5-2)^2 + (6-1)^2 = r^2$$

$$\Rightarrow r^2 = 9 + 25$$

$$\Rightarrow \boxed{r^2 = 34}$$

When it passes through to $B(-3, k)$

$$(-3-2)^2 + (k-1)^2 = 34$$

$$\Rightarrow (k-1)^2 = 34 - 25$$

$$\Rightarrow (k-1) = \pm 3$$

$$\Rightarrow \boxed{k = 4} \text{ or } \boxed{k = -2}$$

(b) P divides the line segment \overline{AB} in the ratio 3:2

ratio. Then by section formula, $A = (-1, 7)$, $B = (4, 3)$

$$P = \left(\frac{3(4) + 2(-1)}{3 + 2}, \frac{3(-3) + 2(7)}{3 + 2} \right) = \left(\frac{mx_2 + nx_1}{m+n}, \frac{my_2 + ny_1}{m+n} \right)$$

$$= (2, 1)$$

By distance formula $(\overline{AB}) = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

$$= \sqrt{(-1-4)^2 + (7-3)^2}$$

$$= \sqrt{25 + 16}$$

$$= 5\sqrt{5} \text{ units}$$

27.

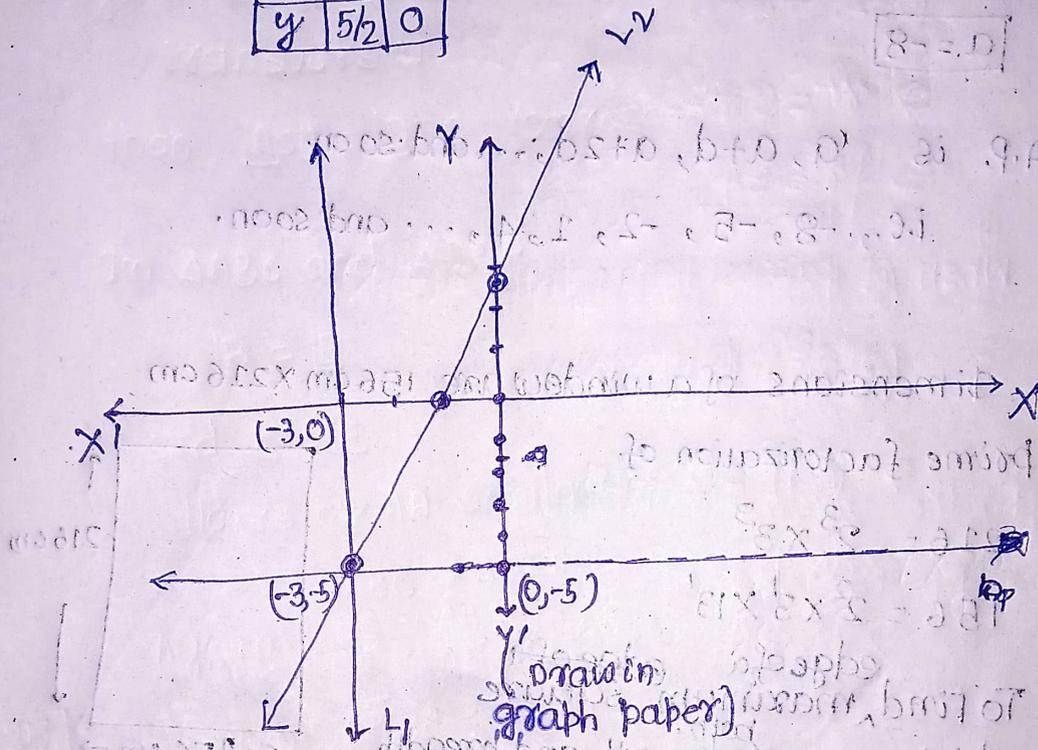
Consider system of linear equations

6

$$L_1: x = -3$$

$$L_2: 5x - 2y = -5$$

x	0	-1
y	5/2	0



Hence solution is $(-3, -5)$.

28. (a)

Let first term = a
common difference = d in an A.P.

$$n\text{th term } (a_n) = a + (n-1)d$$

$$\text{Sum of } n \text{ terms } (S_n) = \frac{n}{2} [2a + (n-1)d]$$

$$\text{ATQ, } a_{15} = a_9 + 21$$

$$\Rightarrow (a + 14d) - (a + 7d) = 21$$

$$\Rightarrow 7d = 21$$

$$\Rightarrow \boxed{d=3}$$

$$\text{Again } S_{10} = 55$$

⇒ $\frac{10}{2} [2a + 9d] = 55$

⇒ $2a + 9(3) = 11$

⇒ $2a = -16$

⇒ $a = -8$

$1 \times x = -3$
 $2 \times x = -6$

1	0	2
0	1	3

∴ A.P. is $a, a+d, a+2d, \dots$ and so on.
i.e., $-8, -5, -2, 1, 4, \dots$ and so on.

29.

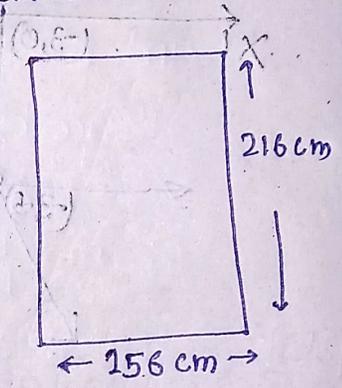
Dimensions of a window are $156 \text{ cm} \times 216 \text{ cm}$

prime factorization of

$216 = 2^3 \times 3^3$

$156 = 2^2 \times 3^1 \times 13^1$

To find ^{edge of a} maximum ^{edge of a} square ^{both} which cover ^{length and breadth}



is $HCF(216, 156) = 2^2 \times 3^1$

Number of such square = $\frac{\text{Area of window}}{\text{Area of a square}}$

$\frac{156 \times 216}{(2^2 \times 3)^2}$

$= \frac{2^2 \times 3 \times 13 \times 2^3 \times 3^3}{2^4 \times 3^2}$

$= 2^1 \times 3^2 \times 13$

$= 284$

$n = 284$

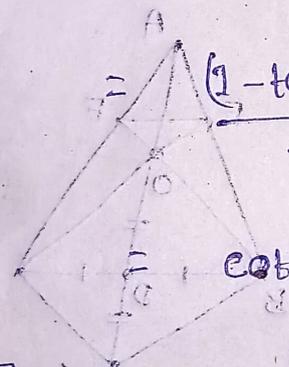
30.

$$\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta}$$

$$= \frac{\tan \theta}{1 - \frac{1}{\tan \theta}} + \frac{\frac{1}{\tan \theta}}{1 - \tan \theta}$$

$$= \frac{-\tan^2 \theta}{1 - \tan \theta} + \frac{1}{\tan \theta(1 - \tan \theta)}$$

$$= \frac{1 - \tan^3 \theta}{\tan \theta(1 - \tan \theta)}$$

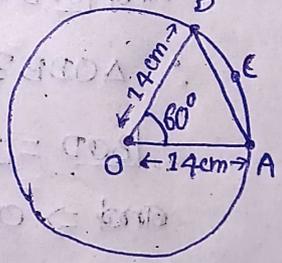


$$= \frac{(1 - \tan \theta)(1 + \tan \theta + \tan^2 \theta)}{\tan \theta(1 - \tan \theta)}$$

$$= \cot \theta + 1 + \tan \theta$$

31.

AB is a chord of a circle where radius (r) = 14 cm making angle 60° with the centre?



$$\text{Area (CAOB sector)} = \frac{\theta}{360^\circ} \times \pi r^2$$

$$= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 14 \times 14$$

$$= \frac{1}{6} \times 22 \times 2 \times 14$$

$$= \frac{1}{3} \times 308$$

$$\approx 102.67 \text{ cm}^2$$

$$\begin{aligned}
 \text{Perimeter of } \widehat{ACB} &= \frac{\theta}{360^\circ} \times 2\pi r \\
 &= \frac{60^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 14 \\
 &= \frac{1}{6} \times 2 \times 22 \times 2 \\
 &= \frac{1}{3} \times 44 \\
 &\approx 14.67 \text{ cm}
 \end{aligned}$$

(9)

SECTION-D

32.

In the given figure given

$$BD = CD \text{ and } OD = GD$$

(i) In $\triangle ODB$ and $\triangle ODG$

$$BD = CD$$

$$OD = OD$$

and $\angle ODB = \angle ODG$ (opposite angle)

$$\therefore \triangle ODB \cong \triangle ODG$$

$$\therefore \angle BOD = \angle DOG \text{ and } OB = OG$$

$$\text{and } \Rightarrow OB \parallel OG \quad \text{--- (i)}$$

Similarly $\triangle ODG \cong \triangle ODC$

$$\therefore \angle DOG = \angle DOC \text{ and } OG = OC$$

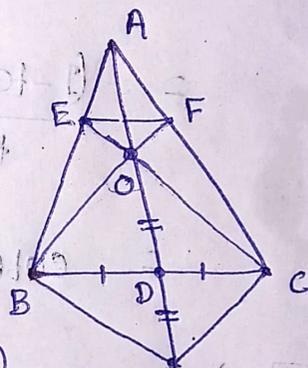
$$\Rightarrow OG \parallel OC \quad \text{--- (ii)}$$

From (i) and (ii) $OBGC$ quadrilateral

two opposite pairs are parallel and same,

so $OBGC$ is a quadrilateral,

Simply as diagonals are bisect each other.



(10)

(ii) In $\triangle ABG$, $EO \parallel BG$. (as given $EO \parallel BG$)

By thales th^m

$$\frac{AE}{BE} = \frac{AO}{BO} \quad \text{--- (i)}$$

and In $\triangle ACG$, $FO \parallel CG$ (as given $BO \parallel CG$)

By thales th^m

$$\frac{AF}{CF} = \frac{AO}{OG} \quad \text{--- (ii)}$$

From (i) and (ii)

$$\frac{AE}{EB} = \frac{AF}{FC}$$

$\Rightarrow EF \parallel BC$. (By Converse of thales th^m)

(iii) As from (ii) $EF \parallel BC$

In $\triangle AEF$ and $\triangle ABC$

$$\angle AEF = \angle ABC$$

and $\angle AFE = \angle ACB$ (Corresponding angle)

Hence by AA similarity criterion

$$\triangle AEF \sim \triangle ABC$$

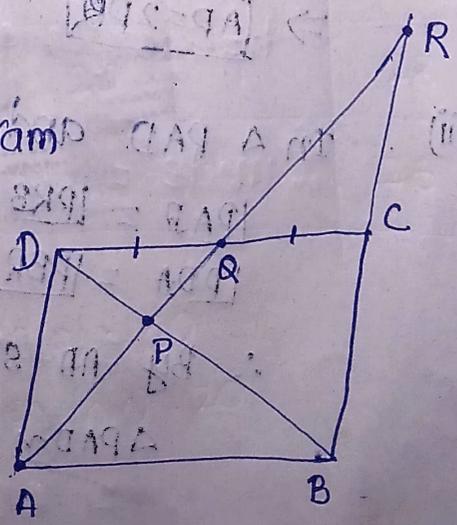
32. (b) Given ABCD is a parallelogram and Q is a mid-point of CD.

In $\triangle AQR$ and $\triangle BQC$

$$\angle QAD = \angle QRC \quad \text{(As } AD \parallel BR \text{)}$$

$$\angle QDA = \angle QCR$$

(Corresponding angle alternate)



∴ By AA similarity criterion

$$\triangle PAD \sim \triangle QRE$$

$$\Rightarrow \frac{QA}{QR} = \frac{AD}{CR} = \frac{QD}{QC}$$

$$\frac{AO}{BO} = \frac{AE}{BE}$$

$$\Rightarrow \frac{QA}{QR} = \frac{AD}{CR} = 1 \quad (\text{AS } QD = QC \text{ and } Q \text{ is a mid-point of } DC)$$

$$\Rightarrow \boxed{QA = QR} \quad \text{and} \quad \boxed{AD = CR}$$

(ii)

In $\triangle PAB$ and $\triangle PQD$

$$\angle PAB = \angle PQD$$

(∵ $AB \parallel QD$ corresponding alternate angle)

$$\text{and } \angle PBA = \angle PQR$$

∴ By AA similarity criterion

$$\triangle PAB \sim \triangle PQD$$

$$\Rightarrow \frac{AP}{PQ} = \frac{PB}{PD} = \frac{AB}{DQ}$$

$$= \frac{2PB}{DQ} \quad (\text{AS } AB = 2DQ)$$

$$\Rightarrow \frac{AP}{PQ} = 2$$

$$\Rightarrow \boxed{AP = 2PQ}$$

(iii)

In $\triangle PAD$ and $\triangle PRB$

$$\angle PAD = \angle PRB$$

(∵ $AD \parallel BR$)

$$\angle PDA = \angle PBR$$

Correspond (Alternate angle)

∴ By AA similarity criterion

$$\triangle PAD \sim \triangle PRB$$

(8)

From (i) $AD = CR$

and $AD = BC$ (as ABCD is a parallelogram)

So $CR = BC$

and $\frac{AD}{BR} = \frac{PD}{PB} = \frac{AP}{RP}$

$\Rightarrow \frac{AP}{RP} = \frac{AD}{BR}$

$= \frac{AD}{BC + CR}$

$= \frac{AD}{2BC}$

$\Rightarrow \frac{AP}{RP} = \frac{1}{2}$ (as $AD = BC$)

$\Rightarrow PR = 2AP$

33. (a)

Given mean $(\bar{x}) = 53$ of the following distribution

Class	f	mc	$x-a$	$u = \frac{x-a}{h}$	uf
0-20	12	10	-40	-2	-24
20-40	15	30	-20	-1	-15
40-60	p	50	0	0	0
60-80	28	70	20	1	28
80-100	13	90	40	2	26

Let assume mean $(a) = 50$

Interval length $(h) = 20$

$\therefore \sum uf = -24 - 15 + 0 + 28 + 26 = 15$

$$\Sigma f = 12 + 15 + p + 28 + 13 = 68 + p$$

(13)

by step deviation method

$$\text{mean} = a + \frac{\Sigma fu}{\Sigma f} \times h$$

$$\Rightarrow 53 = 50 + \frac{15}{68+p} \times 20$$

$$\Rightarrow \frac{300}{68+p} = 3$$

$$\Rightarrow 300 = 204 + 3p$$

$$\Rightarrow 3p = 96$$

$$\Rightarrow \boxed{p = 32}$$

We have ~~for~~ highest frequency $(f_1) = 32$

modal class: 40-60

l = lower limit of the modal class = 40

f_0 = preceding frequency of the modal class = 15

f_2 = succeeding frequency of the modal class = 28

h = length of the modal class = 20

$$\therefore \text{mode} = l + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$$

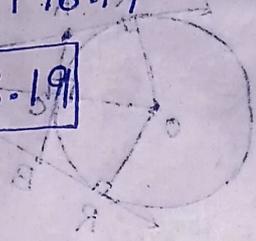
$$= 40 + \frac{32 - 15}{2(32) - 15 - 28} \times 20$$

$$= 40 + \frac{17}{21} \times 20$$

$$= 40 + \frac{340}{21}$$

$$\approx 40 + 16.19$$

$$\Rightarrow \boxed{\text{mode} = 56.19}$$



(b) Given distribution table (Discrete frequency)

mid-value (x)	frequency (f)	Cumulative Frequency (F)
115	12	12
125	15	27
135	20	47
145	16	63
155	10	73
165	16	89
175	11	100
$\frac{92}{9A}$		

$$\text{median} = \frac{\left(\frac{n}{2}\right)^{\text{th}} + \left(\frac{n}{2} + 1\right)^{\text{th}} \text{ observation}}{2}$$

$$= \frac{\left(\frac{100}{2}\right)^{\text{th}} + \left(\frac{100}{2} + 1\right)^{\text{th}} \text{ obsen}}{2}$$

$$= \frac{50^{\text{th}} + 51^{\text{th}} \text{ observation}}{2}$$

$$= \frac{145 + 145}{2} = \frac{290}{2} = 145$$

$$\boxed{\text{median} = 145}$$

34.

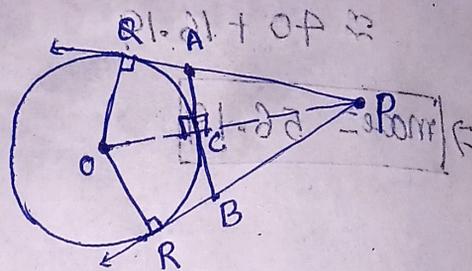
PQ and PR are two tangent.

radius $(r) = 5$ cm.

AB is another tangent at C.

OP = 13 cm

$$\frac{OAE}{15} + OA = 15 \quad (15)$$

Since $OQ \perp PQ$ (By property of tangent)
 $OQ \perp PR$
 $OC \perp AB$ (As line joining centre to the tangent point is \perp to the tangent)

$$\therefore \triangle OPQ \text{ is } \triangle ORT, \quad OQ^2 + PQ^2 = OP^2$$

$$\Rightarrow PQ^2 = 13^2 - 5^2 = 12^2$$

$$\Rightarrow \boxed{PQ = 12} \text{ cm}$$

$$\text{In } \triangle OPA, \cos \angle OPQ = \frac{OQ}{OP}$$

and since $\angle ACP = 90^\circ$

$$\text{In } \triangle APC, \cos \angle CPA = \frac{CP}{AP} \quad (ii)$$

$$\text{Since } OP = OC + CP$$

$$\Rightarrow CP = 13 - 5$$

$$\Rightarrow \boxed{CP = 8} \text{ cm}$$

Since Eqⁿ (i) and (ii) are same

$$\frac{PQ}{OP} = \frac{CP}{AP}$$

$$\Rightarrow \frac{12}{13} = \frac{8}{AP}$$

$$\Rightarrow AP = \frac{8 \times 13}{12}$$

$$\Rightarrow \boxed{AP = \frac{26}{3}} \text{ cm}$$

Now RATACPA, $AC^2 = AP^2 - RP^2$

$$= \left(\frac{26}{3}\right)^2 - 8^2$$

$$= \frac{676 - 576}{9}$$

$$= \frac{100}{9}$$

$$\Rightarrow \boxed{AC = \frac{10}{3}}$$

Hence $\boxed{AB = 2AC = \frac{20}{3} \text{ cm}}$

Method-II

Given PQ and PR are tangent from P to Q and R.

AB is another tangent at C.

$$OQ \perp PQ$$

$$OR \perp PR$$

$$\text{and } OC \perp AB$$

(as line segment joining centre to the tangent point is \perp to the tangent)

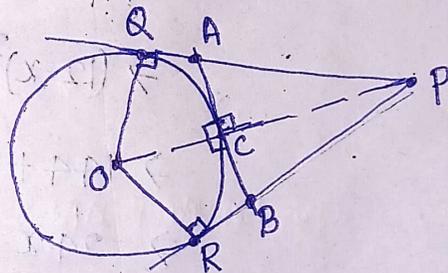
Op = 13 cm and radius = 5 cm

In RAT $\triangle ORP$, $PQ^2 = OP^2 - OQ^2 = 13^2 - 5^2 = 9A$
 $= 169 - 25$

$$\Rightarrow \boxed{PQ = 12 \text{ cm}}$$

$AQ = AC$ and $BC = BR$ and $PQ = PR$

(As length of tangent from an external point to the circle is same)



Let $AQ = x \text{ cm}$

Then $AP = (12 - x) \text{ cm}$

$AQ = x \text{ cm}$

$PC = OP - OC$

$= 13 - 5$

$\Rightarrow PC = 8 \text{ cm}$

$\angle ACO \neq \angle ACP = 90^\circ$

\therefore In $\triangle ACP$, $\angle ACP = 90^\circ$

By Pythagoras theorem

$AP^2 = AC^2 + CP^2$

$\Rightarrow (12 - x)^2 = x^2 + 8^2$

$\Rightarrow 144 + x^2 - 24x = x^2 + 64$

$\Rightarrow 24x = 80$

$\Rightarrow \boxed{x = \frac{10}{3} \text{ cm}}$

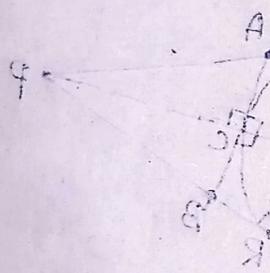
$\boxed{AQ = \frac{10}{3} \text{ cm}}$

So, $AB = 2AC = \boxed{\frac{20}{3} \text{ cm}}$

$AP = 12 - x$

$= 12 - \frac{10}{3}$

$\Rightarrow \boxed{AP = \frac{26}{3} \text{ cm}}$



Method 2

$AR = AC$ and $RC = BR$ and $K = R$

(As radii of circle from an external point to

the circle is same)

35.

18

Let two water tapes are B (with big diameter) and A (with small diameter).

Together A and B fill the tank in $8\frac{8}{9}$ hours.

Suppose tap A fill a tank in x hours and tap B fill the same tank in y hours

in 1 hour A fill $\frac{1}{x}$ part of the tank

and in 1 hour B fill $\frac{1}{y}$ part of the tank

then in 1 hour together they fill $\frac{1}{x} + \frac{1}{y}$ part of the tank.

Time take to fill the tank = $\frac{xy}{x+y}$ hours

$$\Rightarrow 8\frac{8}{9} = \frac{xy}{x+y}$$

Tap B take 4 hours less than A.

$$\text{i.e. } y = x - 4$$

$$\text{From (i)} \quad \frac{80}{9} = \frac{x(x-4)}{x+x-4}$$

$$\Rightarrow 160x - 320 = 9x^2 - 36x$$

$$\Rightarrow 9x^2 - 196x + 320 = 0$$

$$\Rightarrow 9x^2 - 180x - 16x + 320 = 0$$

$$\Rightarrow 9x(x-20) - 16(x-20) = 0$$

$$\Rightarrow (x-20)(9x-16) = 0$$

$$\Rightarrow \boxed{x=20} \text{ or } x = \frac{16}{9} \text{ (impossible)}$$

Hence only possible value of $\boxed{x=20}$

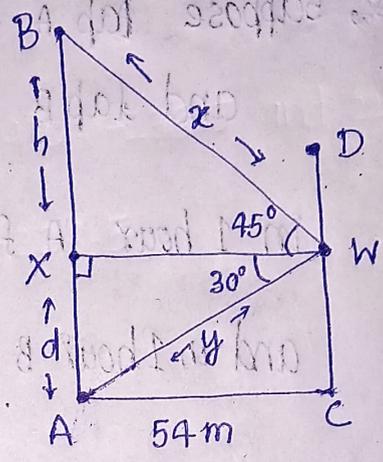
∴ time taken by A is 20 hours and B is 16 hours.

SECTION E

36.

Given AB = elevated water tank
 CD = multi-story building

AC = distance between AB and CD
 = 54 m



From window W

$\angle XWB = \text{angle of elevation} = 45^\circ$

$\angle XWA = \text{angle of depression} = 30^\circ$

(i) $XW = AC = 54 \text{ m}$
 In a RAT ΔAXW , $\cos 30^\circ = \frac{XW}{AW}$
 $\Rightarrow AW = \frac{54}{\sqrt{3}/2}$
 $\Rightarrow y = \frac{108}{\sqrt{3}} \text{ m}$

(ii) In RAT ΔAXW , $\sin 30^\circ = \frac{AX}{AW}$
 $\Rightarrow \frac{1}{2} = \frac{d}{y} \Rightarrow y = 2d$

(iii) In RAT ΔBXW , $\tan 45^\circ = \frac{BX}{XW}$
 $\Rightarrow h = \frac{h}{AC}$
 $\Rightarrow h = 54 \text{ m}$

(iii) (a) In $\triangle AWX$ $\tan 30^\circ = \frac{AX}{XW}$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{d}{54}$$

$$\Rightarrow \boxed{d = 18\sqrt{3} \text{ m}}$$

\therefore height of the water tank $= h + d$
 $= (54 + 18\sqrt{3}) \text{ m}$

(b) In $\triangle XW$, $\cos 45^\circ = \frac{XW}{BW}$

$$\Rightarrow BW = \frac{AC}{\frac{1}{\sqrt{2}}}$$

$$\Rightarrow \boxed{x = 54\sqrt{2} \text{ m}}$$

Height of the window $= d = 18\sqrt{3} \text{ m}$

37

(i)
(ii)

Co-ordinates A = (0, P(0)) = (0, 136).

Span of the Arch = PQ

(21)

$$= 228.5 \frac{b}{a} = 228.5 \frac{1}{5} = 45.7$$

$$= 467.1 \text{ m}$$

(iii) (a) Zeros of the polynomial are -238.5 and 228.5.

$$\text{Sum of zeroes} = -238.5 + 228.5$$

$$-\frac{b}{a} = \frac{-(-0.025)}{-0.0025} = -10$$

Hence sum of zeroes = $-\frac{b}{a}$

(b) $P(100) = -0.0025(100)^2 - 0.025(100) + 136$

$$= -25 - 2.5 + 136$$

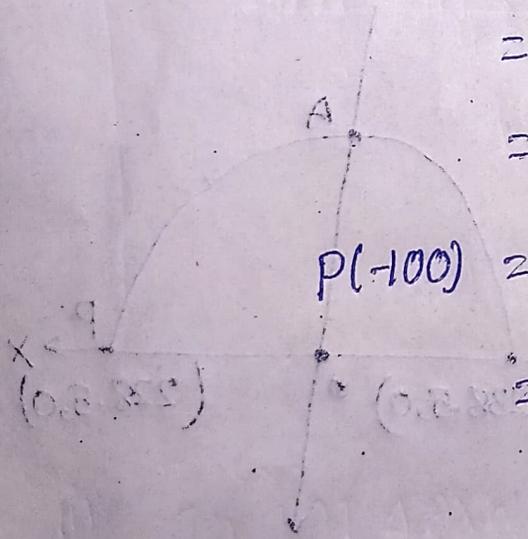
$$= 108.5$$

$$P(-100) = -0.0025(-100)^2 - 0.025(-100) + 136$$

$$= -0.25 + 2.5 + 136$$

$$= 138.25$$

They are not same.



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Dimensions of the cuboid shape wall mounted lamp ?

size $24 \text{ cm} \times 12 \text{ cm} \times 17 \text{ cm}$.

Diameter of a spherical bulb = 7 cm

$$\begin{aligned} \text{(i) Surface area of the bulb} &= 4\pi r^2 \\ &= 4 \times \frac{22}{7} \times \left(\frac{7}{2}\right)^2 \\ &= 154 \text{ cm}^2 \end{aligned}$$

$$\text{(ii) minimum of } (24, 12, 17) = 12 \text{ cm}$$

After left 1 cm space from each side, maximum diameter of the bulb = $12 \text{ cm} - 2 \times 1 \text{ cm} = 10 \text{ cm}$

(iii) (a) If there is a fold of 2 cm on top and bottom edges

then height $(h) = 17 + 2 + 2 = 21 \text{ cm}$

length $(l) = 24 \text{ cm}$ and breadth $(b) = 12 \text{ cm}$

$$\begin{aligned} \text{Surface area} &= 2(l \times h + b \times h) \\ &= 2(24 \times 21 + 12 \times 21) \\ &= 2(504 + 252) \\ &= 1512 \text{ cm}^2 \end{aligned}$$

(b) available space inside lamp

= Volume of the cuboid - volume of the sphere

$$= 17 \times 24 \times 12 - \frac{4}{3}\pi r^3$$

$$= 4896 - 4312$$

$$= 584 \text{ sq. cm.}$$