

SECTION-A

1. (c) 26
2. (c) -36
3. (b) 15^0
4. (d) ± 3
5. (a) 2
6. (c) Infinitely many solutions
7. (b) 8
8. (d) 28
9. (b) $\sqrt{41}$
10. (c) 6.4 cm
11. (d) $1/\sqrt{2}$
12. (b) -1
13. (d) 22 cm
14. (c) 44 cm
15. (d) $R_1^2 + R_2^2 = R^2$
16. (a) a cone and a cylinder
17. (b) 4:3
18. (a) $3 \text{ median} = \text{mode} + 2 \text{ mean}$
19. (A)
20. (d)

Section-B

②

21.

no of students in section-A = 48 and in section-B = 36

Prime factorisation method

$$48 = 2^4 \times 3 \quad \text{and} \quad 36 = 2^2 \times 3^2$$

$$\text{LCM}(48, 36) = 2^4 \times 3^2 = 144$$

Hence minimum no. of books required are 144.

22.(A)

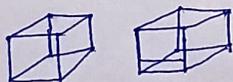
In an A.P. first term $(a) = -3$

$$\begin{aligned} \text{Common difference } (d) &= 2^{\text{nd}} \text{ term} - 1^{\text{st}} \text{ term} \\ &= 4 - (-3) \\ &= 7 \end{aligned}$$

$$\begin{aligned} \text{So } 36^{\text{th}} \text{ term } (T_{36}) &= a + (36-1)d \\ &= -3 + 35(7) \\ &= -3 + 245 \\ &= 242 \end{aligned}$$

23. (B)

Two dice are thrown together.



Sample space $(S) = \{(1,1), (1,2), \dots, (6,6)\}$

$$n(S) = 6 \times 6 = 36$$

E = product of the numbers is 6 in top

$$= \{(1,1), (1,2), \dots\} = \{(1,6), (6,1), (2,3), (3,2)\}$$

$$n(E) = 4$$

$$\therefore P(E) = \frac{n(E)}{n(S)} = \frac{4}{36} = \frac{1}{9}$$

Hence probability of getting product of two dice 6 is $\frac{1}{9}$.

22.(B)

3

Given A.P.: $\sqrt{26}, \sqrt{48}, \sqrt{75}, \dots$

$$1^{\text{st}} \text{ term } (a) = \sqrt{26}$$

For A.P. Common difference should be same.

$$\text{i.e., } \sqrt{48} - \sqrt{26} = \sqrt{75} - \sqrt{48}$$

$$\Rightarrow 2\sqrt{48} = \sqrt{75} + \sqrt{26}$$

$$\Rightarrow 4(48) = 75 + 26 + 2\sqrt{75}\sqrt{26}$$

$$\Rightarrow 192 + 2 \times 5\sqrt{3}\sqrt{26} - 101 = 0$$

$$\Rightarrow 10\sqrt{78} - 91 = 0$$

$$\Rightarrow 100(78) = 91^2 = 8281$$

$$\Rightarrow 7800 = 8281 \text{ (not possible)}$$

Error in the above question

N.B. Grace '2' those has attained it.

23

$$A = 30^\circ \text{ and } B = 60^\circ$$

$$\text{LHS: } \tan(B-A) = \tan(60^\circ - 30^\circ)$$

$$= \tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\text{RHS: } \frac{\tan B - \tan A}{1 + \tan B \cdot \tan A} = \frac{\tan 60^\circ - \tan 30^\circ}{1 + \tan 60^\circ \cdot \tan 30^\circ}$$

$$= \frac{\sqrt{3} - \frac{1}{\sqrt{3}}}{1 + \sqrt{3} \cdot \frac{1}{\sqrt{3}}}$$

$$= \frac{3-1}{\sqrt{3}}$$

$$= \frac{2}{\sqrt{3}}$$

Hence LHS = RHS.

25.(A)

Let $R = (x_0, y_0)$ be a point which divide the line segment joining of $(-1, 7)$ and $(4, -3)$ in $2:3$ ratio.

By section formula

$$x_0 = \frac{2(4) + 3(-1)}{2 + 3} = \frac{5}{5} = 1$$

$$\text{and } y_0 = \frac{2(-3) + 3(7)}{2 + 3} = \frac{15}{5} = 3$$

$$\text{Hence } R(x_0, y_0) = (1, 3).$$

25.(B)

Given points $A = (3, 1)$; $B = (6, 4)$ and $C = (8, 6)$.

$$AB = \sqrt{(6-3)^2 + (4-1)^2} = 3\sqrt{2}$$

(using distance formula)

$$AC = \sqrt{(8-3)^2 + (6-1)^2} = 5\sqrt{2}$$

$$BC = \sqrt{(8-6)^2 + (6-4)^2} = 2\sqrt{2}$$

$$\text{Since } AB + BC = 3\sqrt{2} + 2\sqrt{2} = 5\sqrt{2} = AC$$

Hence A, B and C are collinear.

Section - C

26.

Suppose that $\sqrt{2} + \sqrt{3}$ is rational

$$\text{then } \sqrt{2} + \sqrt{3} = \frac{p}{q}; \text{HCF}(p, q) = 1$$

$$\Rightarrow 2 + 3 + 2\sqrt{6} = \frac{p^2}{q^2}$$

$$\Rightarrow \sqrt{6} = \frac{p^2 - 5q^2}{2q^2} \quad \text{--- } \textcircled{1}$$

Again suppose $\sqrt{6}$ is irrational

$$\Rightarrow \sqrt{6} = \frac{a}{b}; \text{HCF}(a, b) = 1$$

$$\Rightarrow b = \frac{a^2}{b^2}$$

$$\Rightarrow b^2 = \frac{a^2}{6} \text{ ————— (ii)}$$

$$\Rightarrow 6 \mid a^2$$

$$\Rightarrow 6 \mid a \text{ ————— (iii)}$$

$$\Rightarrow a = 6m$$

From (ii) $b^2 = \frac{36m^2}{6}$

$$\Rightarrow b^2 = 6m^2$$

$$\Rightarrow 6 \mid b^2$$

$$\Rightarrow 6 \mid b \text{ ————— (iv)}$$

~~$$\Rightarrow 6 \mid 6$$~~

From (iii) & (iv) $\text{HCF}(a, b) \geq 6$

Which is contradict to our assumption.

so $\sqrt{6}$ is irrational

Which ~~contradict~~ from (i) $\sqrt{6}$ irrational & $\frac{p^2 - 5q^2}{29^2}$ is rational

Which is a contradiction.

Hence $\sqrt{2} + \sqrt{3}$ is irrational.

27.

$$x - y + 1 = 0 \text{ ————— (i)}$$

$$3x + 2y - 12 = 0 \text{ ————— (ii)}$$

$$\text{Eq}^n \text{(i)} \times 2 : 2x - 2y + 2 = 0$$

$$\text{Eq}^n \text{(ii)} \times 1 : 3x + 2y - 12 = 0$$

$$\Rightarrow 5x - 10 = 0$$

$$\Rightarrow \boxed{x = 2}$$

From (i) $y = x + 1$

$$\Rightarrow y = 2 + 1 \Rightarrow \boxed{3 = y}$$

28.(A)

Given $\angle ABD = \angle ACD$

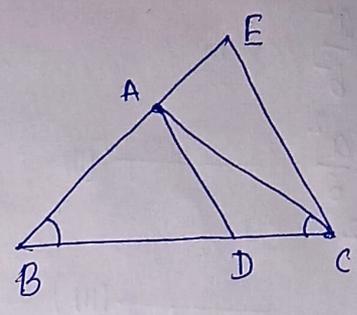
\Rightarrow In $\triangle ABD$
 $AB = AC$

Again $\frac{BC}{BD} = \frac{BE}{AC}$ (given)

$$\Rightarrow \frac{BC}{BD} = \frac{BE}{BA}$$

$\Rightarrow AD \parallel CE$ and $\angle B$ is common.

$\therefore \triangle ABD \sim \triangle EBC$



6

28.(B)

(i) Given $\triangle ABC$ and $\triangle AED$ are right angle triangle

with $\angle ABC = \angle AED = 90^\circ$

$\angle A$ is common

\therefore By AA similarity criterion

$\triangle ABC \sim \triangle AED$

(ii) Corresponding sides are similar

$$\frac{AB}{AE} = \frac{AC}{AD}$$

$$\Rightarrow \boxed{AB \times AD = AC \times AE}$$

29.(A)

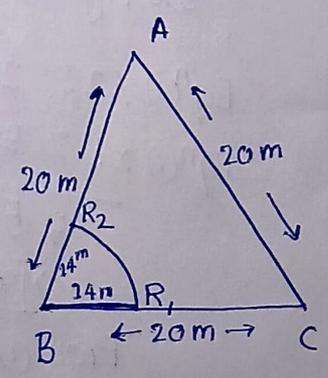
A horse is tied with B corner.

r = length of rope = 14 m.

Area of the Sector BR_1R_2

$$= \frac{\theta}{360^\circ} \times \pi r^2$$

$$= \frac{60^\circ}{360^\circ} \times \frac{22}{7} \times 14^2$$



$$= \frac{1}{6} \times 22 \times 14 \times 2$$

$$= \frac{1}{3} \times 22 \times 14 = \frac{1}{3} \times 308$$

$$\approx 102.67 \text{ Sq.m.}$$

$$\Delta ABC \text{ area} = \frac{1}{2} \times AB \times BC \times \sin A$$

$$= \frac{1}{2} \times 20 \times 20 \times \sin 60^\circ$$

$$= 20 \times 20 \times \frac{\sqrt{3}}{2}$$

$$= 100\sqrt{3}$$

$$\approx 100 \times 1.73$$

$$= 173 \text{ Sq.m.}$$

$$\therefore \text{Area not gaze by horse} = \text{ar}(\Delta ABC) - \text{ar}(\text{Sector } BRP_2)$$

$$= 173 - 102.67$$

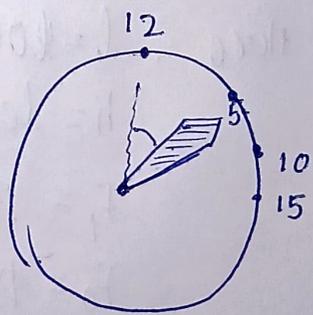
$$= 70.33 \text{ Sq.m.}$$

29.(B)

Angle make by minute hand
in between 8:00 am to 8:05 am

$$\text{is } 5 \times 6^\circ = 30^\circ$$

Length of minute hand (r) = 14 cm



So, area swept by minute hand

$$= \frac{\theta}{360^\circ} \times \pi r^2 = \frac{30^\circ}{360^\circ} \times \pi \times 14^2$$

$$= \frac{30^\circ}{2^\circ} \times 14 \times 14 = 30 \times 7 \times 14$$

$$= 2940 \text{ Sq.cm}$$

30.

$P(x, y)$ any point on the line

L such that $PA = PB$.

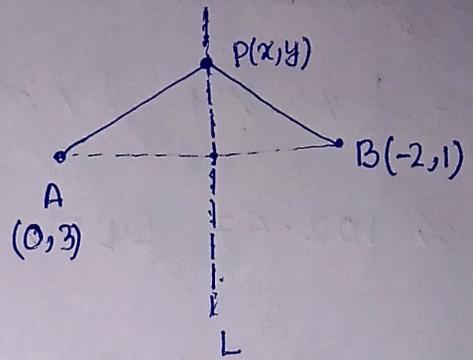
$$\Rightarrow PA^2 = PB^2$$

$$\Rightarrow (x-0)^2 + (y-3)^2 = (x+2)^2 + (y-1)^2$$

$$\Rightarrow x^2 + y^2 + 9 - 6y = x^2 + y^2 + 5 + 4x - 2y$$

$$\Rightarrow 4x + 2y = 4$$

$$\Rightarrow \boxed{2x + y = 2}$$



31.

marks (I)	0-20	20-40	40-60	60-80	80-100
No. of Students (f)	21	25	30	24	10

The above grouped frequency distribution is inclusive
Highest frequency = 30

median class : 40-60

Here l = lower limit of the median class = 40

h = length of median class = 20

f_1 = frequency of the median class = 30

f_0 = preceding frequency of the median class = 25

f_2 = succeeding frequency of the median class = 24

$$\text{median} = l + \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \times h$$

$$= 40 + \frac{30 - 25}{2 \times 30 - 25 - 24} \times 20$$

$$= 40 + \frac{5}{11} \times 20$$

$$= 40 + \frac{100}{11}$$

$$\approx 40 + 9.09$$

$$= 49.09$$

Section-D

32.(A)

Let uniform speed = x km/h and time taken to cover 480 km is t hr.

Since distance = speed \times time

ie. $S = xt$

$$\Rightarrow \boxed{480 = xt} \quad \text{--- (i)}$$

ACQ $(x-8)(t+3) = 480$ --- (ii)

$$\Rightarrow 3x - 8t + xt - 24 = 480$$

$$\Rightarrow 3x - 8t = 24$$

$$\Rightarrow \cancel{x} - \frac{1}{3} \cdot 24 + 8t \Rightarrow \boxed{\frac{1}{8}(3x - 24) = t}$$

From (i) $x \cdot \frac{1}{8}(3x - 24) = 480$ --- (6)

$$\Rightarrow 3x^2 - 24x = 3840$$

$$\Rightarrow x^2 - 8x = 1280$$

$$\Rightarrow x(x-8) = 40 \times 32$$

$$\Rightarrow \boxed{x = 40} \text{ km/h. and reduced speed} = 32 \text{ km/h}$$

(B)

$$x^3 - 4x^2 + 3x + 1 = (x-2)^3$$

$$= x^3 - 3 \times x^2 \times 2 + 3 \times x \times 2^2 - 2^3$$

$$\Rightarrow \boxed{2x^2 - 9x + 9 = 0}$$

$$\Rightarrow 2x^2 - 6x - 3x + 9 = 0$$

$$\Rightarrow 2x(x-3) - 3(x-3) = 0$$

$$\Rightarrow (2x-3)(x-3) = 0$$

$$\Rightarrow \boxed{x = 3/2} \text{ or } \boxed{x = 3}$$

33.

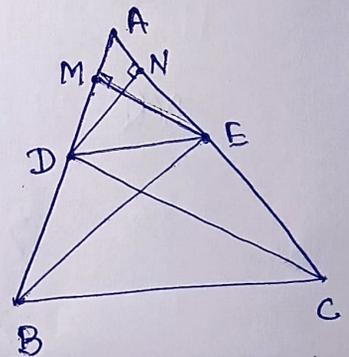
(Basic proportionality theorem)

If a line is drawn parallel to one side of a triangle intersecting the other sides in distinct points, then it divides the other sides in the same ratio.

Given $DE \parallel BC$ in $\triangle ABC$.

Join CD, EB .

Draw $EM \perp AD$ and $DN \perp AE$



Since $ar(\triangle ADE) = \frac{1}{2} \times AD \times EM$ — (i)

$ar(\triangle ADE) = \frac{1}{2} \times AE \times DN$ — (ii)

$\triangle BDE$ and $\triangle CED$ having same base DE and lies in between DE and BC with $BC \parallel DE$.

So $ar(\triangle BDE) = ar(\triangle CED)$

Where $ar(\triangle BDE) = \frac{1}{2} \times BD \times EM$ — (iii)

$ar(\triangle CED) = \frac{1}{2} \times CE \times DN$ — (iv)

Consider $\frac{ar(\triangle ADE)}{ar(\triangle BDE)} = \frac{ar(\triangle ADE)}{ar(\triangle BED)}$

$$\Rightarrow \frac{\frac{1}{2} \times AD \times EM}{\frac{1}{2} \times BD \times EM} = \frac{\frac{1}{2} \times AE \times DN}{\frac{1}{2} \times CE \times DN}$$

$$\Rightarrow \boxed{\frac{AD}{BD} = \frac{AE}{CE}}$$

In this figure

$EG \parallel CB$ in $\triangle ACB$

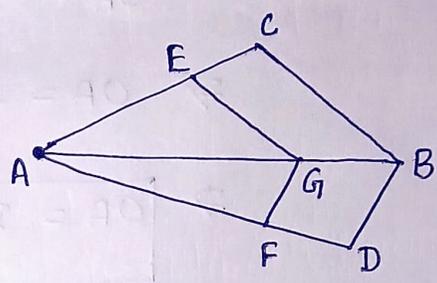
By BPT, $\frac{AE}{EC} = \frac{AG}{GB}$ ——— ①

Again $FG \parallel DB$ in $\triangle ABD$

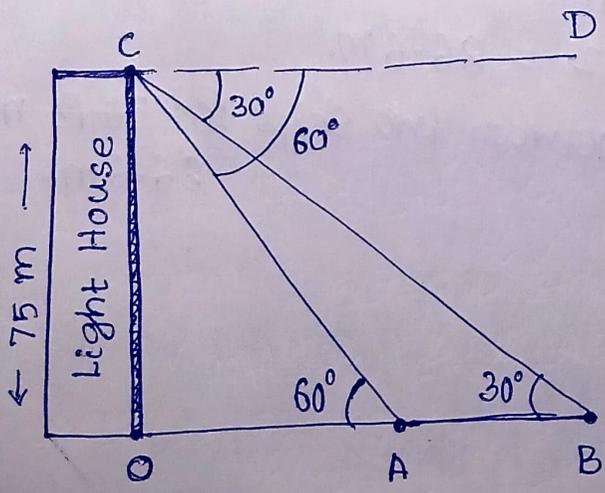
By BPT, $\frac{AF}{FD} = \frac{AG}{GB}$ ——— ②

From ① and ②

$$\frac{AE}{EC} = \frac{AF}{FD}$$



34.



The angle of depression with two ships are respectively 60° and 30° as shown in the figure.

$OC =$ Height of the light house $= 75$ m.

$CD \parallel OB$.

So, $\angle OBC = \angle DCB = 30^\circ$

$\angle OAC = \angle DCA = 60^\circ$

In $\triangle OAC$, $\frac{OC}{OA} = \tan 60^\circ$

$\Rightarrow OA = \frac{75}{\sqrt{3}}$ m

$\Rightarrow OA = \frac{75\sqrt{3}}{3}$ m.

In $\triangle OBC$, $\frac{OC}{OB} = \tan 30^\circ$

$\Rightarrow OB = \frac{75}{\frac{1}{\sqrt{3}}} = 75\sqrt{3}$ m.

$\therefore AB = OB - OA$

$= 75\sqrt{3} - \frac{75}{3}\sqrt{3} = 75\sqrt{3} - 25\sqrt{3}$

$= 50\sqrt{3}$ m

$\approx 50 \times 1.732 = 86.6$ m.

Hence distance between two ships ~~is~~ $50\sqrt{3}$ m.
 86.6 m.

Section-D

35.(A)

Life time (hr) (I)	No. of lamps (f)	x	x-a	$u = \frac{x-a}{h}$	uf
1500 - 2000	14	1750	-1000	-2	-28
2000 - 2500	56	2250	-500	-1	-56
2500 - 3000	60	2750	0	0	0
3000 - 3500	86	3250	500	1	86
3500 - 4000	74	3750	1000	2	148
4000 - 4500	62	4250	1500	3	186
4500 - 5000	48	4750	2000	4	192

Let assumed mean (a) = 2750

h = length of interval = 500

$$\therefore \sum uf = -28 - 56 + 0 + 86 + 148 + 186 + 192$$

$$= 528$$

$$\sum f = 14 + 56 + 60 + 86 + 74 + 62 + 48$$

$$= 400$$

\therefore By step-deviation method

$$\text{mean } (\bar{x}) = a + \frac{\sum uf}{\sum f} \times h$$

$$= 2750 + \frac{528}{400} \times 500$$

$$= 2750 + 132 \times 5 = 2750 + 660$$

$$= 3410$$

3B.(B)

Given data

(14)

Age (in years)	No. of policy holders (f)	Cumulative (C_f) Frequency
15-20	2	2
20-25	4	6
25-30	18	24
30-35	21	45
35-40	33	78
40-45	11	89
45-50	3	92
50-55	6	98
55-60	2	100

Here $N = \Sigma f = 100 \Rightarrow \frac{N}{2} = 50$

\Rightarrow Median class: $(\frac{N}{2})^{th}$ cumulative frequency correspond
 $= 35-40$

$l =$ lower limit of the median class $= 35$

$f =$ frequency of the median class $= 33$

$C_f =$ ^{preceeding} Cumulative frequency of the median class $= 45$

$h =$ length of the median class $= 5$

\therefore median $= l + \frac{\frac{N}{2} - C_f}{f} \times h$

$= 35 + \frac{50 - 45}{33} \times 5$

$= 35 + \frac{25}{33}$

$\approx 35 + 0.75$

$= 35.75$

Section-E

36.

Houses are numbered from 1 to 49.

(i) No. of houses on "Maplewood Avenue" is 49.

(ii) First term of the A.P. $(a) = 1$
common difference $(d) = 1$

(iii) (A) Sum of all house numbers

$S_{49} = \frac{49}{2} [2a + (49-1)d]$

$$= \frac{49}{2} [2(1) + 48(1)]$$

$$= 49 \times 25$$

$$= 1225$$

(ii) (B) House numbers between 15 and 30 are
16, 17, 18, ..., 29.

$$\text{Sum of its} = S_{29} - S_{15}$$

$$= \frac{29}{2} [2a + 28d] - \frac{16}{2} [2a + 15d]$$

$$= \frac{29}{2} [2 + 28] - \frac{16}{2} [2 + 15]$$

$$= 29 \times 15 - 8 \times 17$$

$$= 435 - 136$$

$$= 299$$

37.

Height of the pole = AB = 5m

BD = 4m.

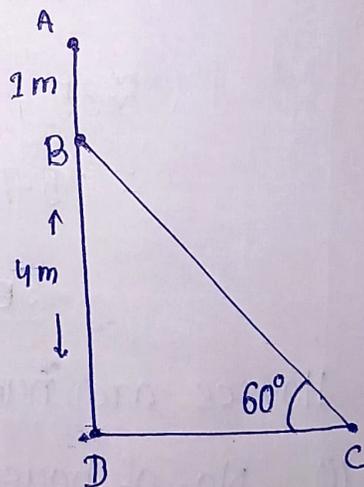
Angle between ladder and land

$$= \angle DCB = 60^\circ$$

$$(i) \sin 60^\circ = \frac{BD}{BC}$$

$$\Rightarrow BC = \frac{4}{\frac{\sqrt{3}}{2}} = \frac{8}{\sqrt{3}}$$

∴ length of the ladder is $\frac{8}{\sqrt{3}}$ m.



(ii) (A) $\tan 60^\circ = \frac{BD}{CD}$

$\Rightarrow CD = \frac{BD}{\tan 60^\circ} = \frac{4}{\sqrt{3}}$

Hence distance between foot of the ladder & foot of the pole = $4/\sqrt{3}$ m.

(B) If $DC = 4$ m, $DB = 4$ m

then $BC = \sqrt{DC^2 + DB^2}$
 $= \sqrt{4^2 + 4^2}$
 $= 4\sqrt{2}$ m

Hence length of the ladder should be $4\sqrt{2}$ m.

38.

Given no of buses (Σf) = 50

(Inclusive Data)

(i)

Distance (I)	No. of Buses (f)	Cf
100-120	12	12
120-140	14	26
140-160	8	34
160-180	6	40
180-200	10	50

Here $N = \Sigma f = 50$

$\frac{N}{2} = 25$

Here median class: 120-140

l = lower limit of the median class = 120

h = length of the interval

c_f = ^{preceeding} cumulative frequency of the median class

= 12

f = frequency of the median class = 14

(ii) Highest Frequency = 14
 ∴ modal class: 120-140

(iii) (A) median = $l + \frac{\frac{N}{2} - C_f}{f} \times h$
 $= 120 + \frac{25 - 12}{14} \times 20$
 $= 120 + \frac{13}{7} \times 10$
 $\approx 120 + 18.57$
 $= 138.57$

(B)

I	f	x	x-a	u = $\frac{x-a}{h}$	uf
100-120	12	110	-40	-2	-24
120-140	14	130	-20	-1	-14
140-160	8	150	0	0	0
160-180	6	170	20	1	6
180-200	10	190	40	2	20

assumed mean (a) = 150
 h = length of interval = 20

$\sum uf = -24 - 14 + 0 + 6 + 20 = -12$
 $\sum f = 50$

∴ $\bar{x} = a + \frac{\sum uf}{\sum f} \times h = 150 + \frac{-12}{50} \times 20$
 $= 150 - \frac{24}{5} = 150 - 4.8 = 145.2$